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398, Ramkrishnapur Road, Barasat  
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## BRAINWARE UNIVERSITY

Term End Examination 2024-2025

Programme – Dip.CE-2024/Dip.CSE-2024/Dip.EE-2024/Dip.ME-2024/Dip.RA-2024

Course Name – Mathematics - I

Course Code - DBS00001

( Semester I )

Full Marks : 60

Time : 2:30 Hours

[The figure in the margin indicates full marks. Candidates are required to give their answers in their own words as far as practicable.]

### Group-A

(Multiple Choice Type Question)

1 x 15=15

1. Choose the correct alternative from the following :

- (i) If  $C = \begin{vmatrix} 1 & 2 & 3 \\ -3 & 0 & -1 \\ 5 & -6 & 7 \end{vmatrix}$ , then identify the co-factor of the element 2.

- a) 6                          b) -16  
c) 14                          d) 16

- (ii) Select the value of  $\lim_{x \rightarrow 3} \frac{x-3}{x^2-2x-3}$ .

- a) 0                          b) 1  
c)  $\frac{1}{4}$                           d) none

- (iii) If  $\tan \theta = 3$ , then select the value of  $\cos 2\theta$ .

- a)  $-\frac{4}{5}$                           b)  $\frac{4}{3}$   
c)  $\frac{1}{3}$                                   d)  $\frac{2}{3}$

- (iv) Select the value of  $2 \sin 30^\circ \cos 30^\circ$ .

- a)  $\frac{1}{2}$                           b) 1  
c)  $\frac{\sqrt{3}}{2}$                           d) none

- (v) Select the value of  $\sin\left(x - \frac{\pi}{2}\right)$ .

a)  $\sin x$

c)  $\cos x$

(vi) If  $\sin x = \frac{3}{4}$  then select the value of  $\cos x$ .

a)  $\frac{2}{3}$

c)  $\frac{\sqrt{7}}{4}$

b)  $-\sin x$

d)  $-\cos x$

b)  $\frac{\sqrt{3}}{2}$

d)  $\frac{1}{2}$

(vii) Identify the value of  $\begin{vmatrix} 3 & 2 \\ 2 & 1 \end{vmatrix}$ .

a) 0

c) 19

b) -1

d) none

(viii) Identify the nature of the matrix  $\begin{pmatrix} 2 & 0 \\ 6 & 9 \end{pmatrix}$ .

a) a diagonal matrix

c) a lower triangular matrix

b) an upper triangular matrix

d) a symmetric matrix

(ix) If  $\begin{bmatrix} x+3 & x+2y \\ z-1 & 4t-6 \end{bmatrix} = \begin{bmatrix} 0 & 7 \\ 3 & 2t \end{bmatrix}$ , then identify the value of x, y, z, t are respectively.

a) 3, -2, -4, 3

c) -3, 2, 4, -3

b) -3, 5, 4, 3

d) none

(x)

Choose the value of the determinant  $\begin{vmatrix} 1 & \cos 60^\circ & \cos 30^\circ \\ \frac{1}{2} & \sin 30^\circ & \sin 60^\circ \\ 1 & 0 & 2 \end{vmatrix}$

a)  $\frac{\sqrt{3}}{2}$

c) 0

b)  $\frac{1}{2}$

d) none

(xi) Choose the nature of the transpose of a square matrix from below options.

a) scalar matrix

c) diagonal matrix

b) square matrix

d) rectangular matrix

(xii) If the difference of the roots of the  $x^2 + px + 8 = 0$  be 2 then select the value of p.

a)  $\pm 4$

c)  $\pm 9$

b)  $\pm 10$

d)  $\pm 6$

(xiii) If  $x = a \cos t$  and  $y = b \sin t$ , then calculate the value of  $\frac{dy}{dx}$ .

a)  $\frac{b}{a} \cot t$

c)  $-\frac{b}{a} \cot t$

b)  $\frac{a}{b} \cot t$

d)  $\frac{b}{a} \tan t$

(xiv) Calculate the value of  $\frac{d}{dx} (\sin x^0)$ .

a)  $\cos x^0$

c)  $\cos \frac{x}{\pi}$

b)  $\cos x$

d)  $\frac{\pi}{180} \cos x^0$

- (xv) If  $y = \left(-\frac{b}{a} \cot t\right)x$ , then calculate the value of  $\frac{dy}{dx}$ .
- a)  $\frac{b}{a} \cot t$   
 b)  $\frac{a}{b} \cot t$   
 c)  $-\frac{b}{a} \cot t$   
 d)  $\frac{b}{a} \tan t$

**Group-B**  
 (Short Answer Type Questions)

$3 \times 5 = 15$

2. Identify the value of the limit:  $\lim_{x \rightarrow 1} \frac{x^2 - 1}{\sqrt{5x-1} - \sqrt{3x+1}}$  (3)
3. Identify the value of the limit:  $\lim_{x \rightarrow 1} (x^3 + 3x + 6)$  (3)
4. Identify the area of the triangle with vertices A (1,1,2), B (2,3,5) and C (1,5,5). (3)
5. Show that,  $\tan 35^\circ + \tan 10^\circ + \tan 35^\circ \cdot \tan 10^\circ = 1$ . (3)
6. Evaluate the value of  $\frac{d}{dx} (e^x \cos x)$ . (3)

OR

- Evaluate the value of  $\frac{d}{dx} (x^2 \sin x)$ . (3)

**Group-C**  
 (Long Answer Type Questions)

$5 \times 6 = 30$

7. Let, (5)

$$f(x) = \begin{cases} x & x \geq 0 \\ -x & x < 0 \end{cases}$$

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Examine that  $f(x)$  is continuous at  $x=0$ .

8. Evaluate the sum of two given vectors  $i-2j+3k$  and  $3i-2j+k$ . (5)

9. Show that any square matrix can be uniquely expressed as the sum of a symmetric and a skew-symmetric matrix. (5)
10. If the co-ordinate of two points A and B are  $(1,6,5)$  and  $(-7,5,2)$  respectively then identify the value of  $\vec{AB}$ . (5)
11. Examine the nature of the roots of the equation  $3x^2 - 10x + 3 = 0$ . (5)
12. If  $B = \begin{pmatrix} -1 & 3 & 5 \\ 1 & -3 & -5 \\ -1 & 3 & 5 \end{pmatrix}$  and  $C = \begin{pmatrix} 2 & -2 & 4 \\ -1 & 3 & 4 \\ 1 & -2 & -3 \end{pmatrix}$ , evaluate the value of  $6B+C$ . (5)
- OR
- If  $B = \begin{pmatrix} -1 & 3 & 5 \\ 1 & -3 & -5 \\ -1 & 3 & 5 \end{pmatrix}$  and  $C = \begin{pmatrix} 2 & -2 & 4 \\ -1 & 3 & 4 \\ 1 & -2 & -3 \end{pmatrix}$ , evaluate the value of  $B-6C$ . (5)

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