

## **BRAINWARE UNIVERSITY**

## **Term End Examination 2022**

Programme - Dip.CSE-2018/Dip.EE-2018/Dip.ECE-2019/Dip.CSE-2019/Dip.ME-2019/Dip.CSE-2020/Dip.CSE-2021/Dip.EE-2021/Dip.ME-2021/Dip.CSE-2022/Dip.ME-2022/Diploma in Robotics & Automation-2022/Dip.EE-2022/Dip.CE-2022

Course Name - Mathematics I/Mathematics-I

Course Code - DMAT010101/DECE104/DCSE104/DME104/DEE104/BS102

(Semester I)

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Time: 2:30 Hours

[The figure in the margin indicates full marks. Candidates are required to give their answers in their own words as far as practicable.]

Group-A

(Multiple Choice Type Question)

1 x 15=15

1. Choose the correct alternative from the following:

(i) Observe the value of  $\log_8^{\sqrt{8}}$  =

a) 1/3

c) 1/2

(ii)

b) 1/4

d) 1/8

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If  $x = a \sec^2 \theta$ ,  $y = b \tan^2 \theta$ , then write the value of  $\frac{dy}{dx} = \frac{dy}{dx}$ 

a) a/b

c) ab

d) b/a

If  $x = a\cos t$  and  $y = b\sin t$ , then write the value of  $\frac{dy}{dt} =$ 

 $\frac{b}{-\cot t}$ 

 $-\frac{b}{\cot t}$ 

 $\frac{a}{b}$  cot t

(iv) If  $y = \tan^{-1} \frac{\cos x}{1 + \sin x}$ , then evaluate  $\frac{dy}{dx} =$ 

a) 1 c) -1/2

b) 1/2 d) 2

(v) Evaluate  $\frac{d}{dx} \left\{ \cos^{-1} \frac{x}{5} \right\} =$ 

b)

If  $C = \begin{vmatrix} 1 & 2 & 3 \\ -3 & 0 & -1 \\ 5 & -6 & 7 \end{vmatrix}$ , then evaluate the co-factor of the element 2 is

- Determine the value of | 1 1 1 | 4 6 9 | 5 6 7 |
- b) -16
  d) 16

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- a) 0 c) 19
  - Determine the value of  $\begin{vmatrix} 1 & -2 & 3 \\ 2 & -1 & 4 \\ -2 & 3 & 1 \end{vmatrix}$
- b) -1 d) none
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(ix)

(x)

Deetermine the value of  $\begin{vmatrix} 1 & 2 & 3 \\ 0 & 5 & 6 \\ 4 & 6 & 8 \end{vmatrix}$ 

- b) 13
- d) none

- b) 1 d) none of these
- If  $A = \begin{bmatrix} 0 & -1 \\ 1 & 3 \\ 2 & 0 \end{bmatrix}$ , then evaluate  $2A^{T} = \begin{bmatrix} 0 & -1 \\ 1 & 3 \\ 2 & 0 \end{bmatrix}$
- a)
- $\begin{bmatrix} 0 & 2 & 4 \\ -2 & 6 & 0 \end{bmatrix}$

 $\begin{bmatrix} 0 & -2 \\ 2 & 6 \\ 4 & 0 \end{bmatrix}$ 

c)

$$\begin{bmatrix} 0 & 1 & 2 \\ -2 & 6 & 0 \end{bmatrix}$$

- $\begin{pmatrix}
  0 & -1 \\
  1 & 3 \\
  4 & 0
  \end{pmatrix}$
- If the co-ordinate of two points A and B are (1,0,5) and (-1,5,2) respectively then Identify the value of  $\overrightarrow{AB} =$

$$^{a)}5i+7k$$

$$-2i+5j-k$$

c) 
$$3i+2j-k$$

 $^{(d)}-2i+5j-3k$ 

<sup>(</sup>xii) Select the correct value for logarithm of 1728 to the base  $2\sqrt{3}$ 

(xiii) Identify the vector in the direction of the vector  $\vec{a} = \hat{i} - 2\hat{j} + 2\hat{k}$  that has magnitude

$$\hat{i}-2\hat{j}+2\hat{k}$$

$$3\left(\hat{i}-2\hat{j}+2\hat{k}\right)$$

 $\frac{1}{3} \left( \hat{i} - 2 \hat{j} + 2 \hat{k} \right)$   $9 \left( \hat{i} - 2 \hat{j} + 2 \hat{k} \right)$ 

If  $\sin x = \frac{3}{4}$  then identify the value of  $\cos x$ 

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If  $\log_x^{81} = 4$  then tell the value of x=

c) 3

b) 2

Group-B (Short Answer Type Questions)

3 x 5=15

Show that  $(1-\omega)(1-\omega^4)(1-\omega^2)(1-\omega^5) = 9$ .

Rewrite  $\left(\frac{1+i}{1-i}\right)^3$  in the form A + iB where A and B are real numbers.

(3)

Justify that the points  $\overrightarrow{A} = -2 \overrightarrow{i} + 3 \overrightarrow{j} + 5 \overrightarrow{k}$ ,  $\overrightarrow{B} = \overrightarrow{i} + 2 \overrightarrow{j} + 3 \overrightarrow{k}$  and  $\overrightarrow{C} = 7 \overrightarrow{i} - \overrightarrow{k}$  are collinear.

(3)

(3)

Write the area of the triangle with vertices A(1,1,2), B(2,3,5) and C(1,5,5).

(3)

4. Establish that each of the given three vectors is a unit vector:

(3)

$$\frac{1}{7} \left( \hat{2}i + 6\hat{j} + 6\hat{k} \right), \frac{1}{7} \left( 3\hat{i} - 6\hat{j} + 2\hat{k} \right), \frac{1}{7} \left( 6\hat{i} + 2\hat{j} - 3\hat{k} \right).$$

Using vectors, write the value of k such the points (k,-10,3),(1,-1,3) and (3,5,3) at collinear.

(3)

Evaluate 
$$\frac{dy}{dx}$$
 when  $y = \sqrt{\frac{\sec x - \tan x}{\sec x + \tan x}}$ .

Evaluate the limit:  $\lim_{x\to 1} \frac{x^2-1}{\sqrt{5x-1}-\sqrt{3x+1}}$ .

(3)

(3)

Write the value of 
$$\frac{dy}{dx}$$
 if  $y = \tan^{-1} \sqrt{\frac{1-x}{1+x}}$ 

Let  $f(x) = \frac{x^2 - 1}{x^3 - 1}$ ,  $x \ne 1$ . Write the value of f(x) at x=1 such that f(x) be (3) continuous at x=1?

If vectors  $\overrightarrow{a}$ ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$  are such that  $\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c} = 0$ ,  $|\overrightarrow{a}| = 3$ ,  $|\overrightarrow{b}| = 5$  and  $|\overrightarrow{c}| = 7$  tell the angle between  $\vec{a}, \vec{b}$ .

Visualize the equation of straight line which passes through the point (1, -2) (5) and cuts off equal intercepts from axes?

If 
$$\frac{\log x}{\text{ry-qz}} = \frac{\log y}{\text{pz-rx}} = \frac{\log z}{\text{qx-py}}$$
 show that  $x^p y^q z^r = 1$ .

Show that 
$$\begin{vmatrix} 1+a & 1 & 1 & 1 \\ 1 & 1+b & 1 & 1 \\ 1 & 1 & 1+c & 1 \\ 1 & 1 & 1 & 1+d \end{vmatrix} = abcd \left(1+\frac{1}{a}+\frac{1}{b}+\frac{1}{c}+\frac{1}{d}\right)$$
(5)

9.

If  $\sin^4 \theta + \sin^2 \theta = 1$  establish that  $\tan^2 \theta - \tan^4 \theta + 1 = 0$ .

Establish that 
$$\sqrt{\frac{\cos \cot x + 1}{\csc x - 1}} = \frac{\cos x}{1 - \sin x}$$
.

10. 
$$f(x) = x x \ge 0$$
Let  $-x x \le 0$ 

Analyze that f(x) is continuous at x=0 but not derivable at that point.

Find, from definition, evaluate the derivative of 
$$\log 2x$$
 (5)

If 
$$f(x) = \log \frac{1+x}{1-x}$$
 deduce that  $f\left(\frac{2x}{1+x^2}\right) = 2f(x)$ .

Evaluate 
$$\frac{dy}{dx}$$
 if  $y = x^2 \sqrt{\frac{x^2 - x + 1}{x^2 + x + 1}}$  (5)

<sup>12.</sup> Evaluate the value of k, so that the function f defined below is continuous at  $^{(5)}$ 

x=0, where 
$$f(x) = \begin{cases} \frac{\sqrt{1+kx} - \sqrt{1-kx}}{x}, & -1 \le x < 0 \\ \frac{2x+1}{x-1}, & 0 \le x < 1 \end{cases}$$

Evaluate the value of K for which the function  $f(x) = \begin{cases} Kx^2 + 2x, & x < 2 \\ Kx^3, & x \ge 2 \end{cases}$  is continuous at x=2.

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