



## BRAINWARE UNIVERSITY

### Term End Examination 2018 - 19

Programme – Master of Computer Applications

Course Name – Formal Language and Automata Theory

Course Code - MCA203 / MCA203(BL)

(Semester – 2)

**Time allotted: 3 Hours**

**Full Marks : 70**

[The figure in the margin indicates full marks. Candidates are required to give their answers in their own words as far as practicable.]

### Group –A

(Multiple Choice Type Question)

10 x 1 = 10

1. Choose the correct alternative from the following

(i) A solution of the equation  $R=Q+RP$  is

- |             |             |
|-------------|-------------|
| a. $R=QP^*$ | b. $Q=RP^*$ |
| c. $P=RQ^*$ | d. $R=PQ^*$ |

(ii) Which of the following set is a regular?

- |  |                                 |
|--|---------------------------------|
| a. $\{a^i:i=n^2,n>1\}$                 | b. $\{a^p:p \text{ is prime}\}$ |
| c. $\{ww:w \text{ is in } \{a,b\}^*\}$ | d. $\{a^{2n}:n>=1\}$            |

(iii) A finite automaton accepts which type of language:

- |           |           |
|-----------|-----------|
| a. Type 0 | b. Type 1 |
| c. Type 2 | d. Type 3 |

(iv) Arden's theorem is true for:

- |                                 |                          |
|---------------------------------|--------------------------|
| a. More than one initial states | b. Null transitions      |
| c. Non-null transitions         | d. None of the mentioned |

(v) The value of  $L(\Phi^*)$  is

- |             |                   |
|-------------|-------------------|
| a. $\Sigma$ | b. $\{\epsilon\}$ |
| c. $\{\}$   | d. None of these  |

- (vi) Pumping Lemma for CFL is used to show that
- A given language is regular
  - A given language is Context Free
  - A given language is Context Sensitive
  - None of these
- (vii) The basic limitation of the finite state machine is that
- It cannot remember arbitrary large amount of information
  - It cannot recognize grammars that are regular
  - It sometimes recognize grammars that are not regular
  - All of these
- (viii) Production Rule:  $aAb \rightarrow agb$  belongs to which of the following category?
- Regular Language
  - Context free Language
  - Context Sensitive Language
  - Recursively Enumerable Language
- (ix) Which of the expression is appropriate?  
For production  $p: a \rightarrow b$  where  $a \in V$  and  $b \in \underline{\hspace{2cm}}$
- $V$
  - $S$
  - $(V+\Sigma)^*$
  - $V+\Sigma$
- (x) For  $S \rightarrow 0S1 | \epsilon$  for  $\Sigma = \{0,1\}^*$ , which of the following is wrong for the language produced?
- $0^n 1^n \mid n \geq 0$
  - $0^n 1^n \mid n \geq 1$
  - Non regular language
  - None of these

### Group – B

(Short Answer Type Questions)

3 x 5 = 15

Answer any *three* from the following

- State and prove the Arden's theorem. 5
- List any four closure properties of regular languages. 5
- Show that the following grammar is ambiguous- 5  
 $S \rightarrow aSbS \mid bSaS \mid \epsilon$
- What is unrestricted grammar? Give an example. 5
- Give the formal definition of Finite Automata. 5

**Group – C**

(Long Answer Type Questions)

3 x 15 = 45

Answer any *three* from the following

7. (a) Prove that the family of regular languages is closed under the following operations: 5
- i) Union.
- ii) Intersection.
- iii) Complementation.
- iv) Reversal.
- v) Concatenation.
- (b) Define the following terms: (i) Useless symbol. (ii) Null – production. (iii) Unit production. 6
- (c) Remove Null – productions in the following grammar. 4
- $S \rightarrow ABaC$
- $A \rightarrow BC$
- $B \rightarrow B|\epsilon$
- $C \rightarrow D|\epsilon$
- $D \rightarrow \epsilon$
8. (a) Write the procedure to convert a given CFG into equivalent grammar in CNF. 7
- (b) Let  $G$  be the grammar  $S \rightarrow 0B|1A, A \rightarrow 0|0S|1AA, B \rightarrow 1|1S|0BB$ . For the string 00110101, find: (i) The leftmost derivation. (ii) The rightmost derivation. (iii) The derivation tree. 3+3+2
9. (a) Let  $G$  be  $S \rightarrow AB, A \rightarrow \alpha, B \rightarrow C|b, C \rightarrow D, D \rightarrow E, E \rightarrow \alpha$ . Eliminate unit productions and get an equivalent grammar. 5

- (b) Draw the merger graph, merger table, compatibility graph and then minimize the following machine. 3+3+2+2

Present State	Next State, o/p		Next State , o/p	
	I/p=0	i/p=1	i/p=2	i/p=3
A	-	C,1	E,1	B,1
B	E,0	-	-	-
C	F,0	F,1	-	-,1
D	-	-	B,1	-
E	-	F,0	A,0	D,-
F	C,-	-	B,0	C,1

10. (a) Construct a PDA that recognizes strings (over alphabet 0 and 1) that contain equal number of 0s and 1s. 8
- (b) Explain the concept of Universal Turing Machine. 7
11. (a) What are undecidable problems? Explain why PCP problem is considered undecidable. 4+4
- (b) Write variations of Turing machine. 7

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