



BRAINWARE UNIVERSITY

Term End Examination 2021 - 22
Programme – Bachelor of Computer Applications
Course Name – Discrete Structures
Course Code - GEBS201
(Semester II)

Time allotted : 1 Hrs.15 Min.

Full Marks : 60

[The figure in the margin indicates full marks.]

Group-A

(Multiple Choice Type Question)

$1 \times 60 = 60$

Choose the correct alternative from the following :

(1) Let p: It is cold and q: It is raining , then the symbolic form of the statement ‘It is cold or it is not raining’ is

- | | |
|---------------|--------------------|
| a) $p \vee q$ | b) $\neg p \vee q$ |
|---------------|--------------------|

- | | |
|----------------------|--------------------|
| c) $\neg p \wedge q$ | d) $p \vee \neg q$ |
|----------------------|--------------------|

(2) Let p be a proposition ‘ He is intelligent’ and q be a proposition ‘ He is tall’ . The symbolic form of the statement ‘ He is intelligent and tall’ is

- | | |
|-----------------|----------------------|
| a) $p \vee q$ | b) $\neg p \wedge q$ |
| c) $p \wedge q$ | d) none of these . |

(3) For the statement p and q $\neg(p \vee q)$ is

- | | |
|---------------------------|-------------------------|
| a) $\neg p \wedge \neg q$ | b) $\neg p \vee \neg q$ |
| c) $p \vee q$ | d) none of these . |

(4) $p \vee(p \wedge q) \equiv$

- | | |
|-----------------|------------------|
| a) p | b) q |
| c) $p \wedge q$ | d) none of these |

(5) $p \rightarrow q \equiv$

- | | |
|----|----|
| a) | b) |
|----|----|

$$\neg q \vee \neg p$$

$$\neg p \wedge q$$

c) $\neg p \vee q$

d) $p \vee q$

(6) If the truth value of p and q are F and F respectively then the truth value of $\neg p \rightarrow \neg q$ is

- a) T
c) both T and F

- b) F
d) None of these

(7) If $p \leftrightarrow q \equiv (p \rightarrow q) \wedge r$ then r is

- a) $p \rightarrow q$
c) $q \rightarrow p$

- b) $\neg p$
d) $\neg q$

(8) $\neg(p \vee q) \vee (p \wedge \neg q) \equiv$

- a) $\neg p$
c) $\neg q$

- b) p
d) None of these .

(9) The proposition $p \wedge (q \wedge \neg q)$ is a

- a) contradiction
c) an argument

- b) Tautology
d) none of these .

(10) Contrapositive of ' $\neg p \rightarrow q$ ' is

- a) $p \rightarrow q$
c) $\neg q \rightarrow p$

- b) $\neg q \rightarrow \neg p$
d) $q \rightarrow \neg p$

(11) Let p: 'It is sunny afternoon' and q: 'It is hot today'. Then the following proposition $\neg p \wedge \neg q$ can be written as

- a) It is not sunny afternoon and it is not hot today
. .
c) It is false that It is sunny afternoon or it is hot today .

- b) It is false that It is not sunny afternoon or it is not hot today .
d) None of these .

(12) The negation of the statement 'No one wants to buy my house' is

- a) All want to buy my house
c) Every one wants to buy my house

- b) Some one wants to buy my house
d) None of these .

(13) 'Any proposition' \vee 'a tautology'

- a) The proposition
c) contradiction

- b) tautology
d) none of these

(14) If ${}^{2n}C_3 : {}^nC_2 = 44 : 3$ then the value of n is

- a) 6
c) 2

- b) 5
d) 7

(15) The number of three digit number that can be formed from the digits 1,3,5,7 is,

- a) 24
c) 4

- b) 6
d) none of these

(16) In how many ways 7 different beads can be arranged to form a necklace?

- a) 250
- b) 300
- c) 360
- d) 350

(17) The generating function for the sequence $<1, -1, 1, -1, \dots>$ is

- a) $(1-x)^{-1}$
- b) $(1+x)^{-1}$
- c) $(1+2x)^{-\frac{1}{2}}$
- d) $(1-2x)^{-\frac{1}{2}}$

(18) If $a_n = a_{n-1} + 9$, $n \geq 1$ and $a_0 = 5$ then $a_n =$

- a) $9+5n$
- b) $5+9n$
- c) $9n$
- d) $5n$

(19) The sequence represented by the function $\frac{1}{1-5x}$ is

- a) $\{3^n\}$
- b) $\{5^n\}$
- c) $\{5^n + 1\}$
- d) $\{4^n\}$

(20) If nC_1 , nC_2 and nC_3 are in A.P., the value of n is

- a) 6
- b) 7
- c) 8
- d) 4

(21) If A and B are sets and $A \cup B = A \cap B$, then

- a) $A = \Phi$
- b) $B = \Phi$
- c) $A = B$
- d) none of these

(22) Let R be a non-empty relation on a collection of sets defined by ARB if and only if $A \cap B = \emptyset$, then

- a) R is reflexive and transitive.
- b) R is symmetric and not transitive.
- c) R is an equivalence relation.
- d) R is not reflexive and not symmetric.

(23) Order of the power set of a set of order n is

- a) n
- b) $2n$
- c) n^2
- d) 2^n

(24) Which of the following two sets are equal?

- a) $A = \{1, 2\}$ and $B = \{1\}$
- b) $A = \{1, 2\}$ and $B = \{1\}$
- c) $A = \{1, 2, 3\}$ and $B = \{2, 1, 3\}$
- d) $A = \{1, 2, 4\}$ and $B = \{1, 2, 3\}$

(25) A function from A to B is called onto function if its range is

- a) B
- b) A
- c) Neither A nor B
- d) Both A and B

(26) The smallest set A such that $A \cup \{1, 2\} = \{1, 2, 3, 5, 9\}$ is

- a) $\{2,3,5\}$ b) $\{1, 2, 5, 9\}$
 c) $\{3, 5, 9\}$ d) None of the mentioned
- (27) Let N be the set of all natural numbers, $A = \{x \mid x \in N, x \geq 4\}$ and
 $B = \{x \mid x \in N, x < 5\}$. Then $A \cap B = ?$
- a) $\{4,5\}$ b) $\{4\}$
 c) $\{0\}$ d) $\{9\}$
- (28) If k is a positive integer, then $\gcd(ka, kb) =$
- a) $k \gcd(a, b)$ b) $k \gcd(a, b)$
 c) $\gcd(a, kb)$ d) none
- (29) Set consisting of all first elements of each ordered pair in relation is called
- a) subset b) domain of relation
 c) range of relation d) complement of a set
- (30) Set consisting of all second elements of each ordered pair in relation is called
- a) domain of relation b) range of relation
 c) subset d) complement of a set
- (31) What is the base case for the inequality $7^n > n^3$, where $n = 3$?
- a) $652 > 189$ b) $42 < 132$
 c) $343 > 27$ d) $42 \leq 431$
- (32) If $f(x-2) = 2x^2 + 3x - 5$ then $f(-1) =$
- a) 0 b) 1
 c) -1 d) 2
- (33) The function $f: R \rightarrow R$ defined by $f(x) = x^2$, where R is the set of all real numbers.
 Then f is
- a) surjective b) injective
 c) bijective d) None of these
- (34) If $\phi(x-2) = 2x^2 + 3x - 5$ then $\phi(x) =$
- a) $2x^2 + 11x + 9$ b) $2x^2 - 11x + 9$
 c) $x^2 + 11x + 9$ d) none
- (35) Let a and b any two positive integers. Then
- a) $\gcd(a, b) = \text{lcm}(a, b)$ b) $\gcd(a, b)\text{lcm}(a, b) = ab$
 c) $\gcd(a, b)\text{lcm}(a, b) = 1$ d) $\gcd(a, b)\text{lcm}(a, b) = a + b$
- (36) If $32 \equiv a \pmod{7}$. Then the value of a is-
- a) 10 b) 11

c) 12

d) 13

(37) If $\gcd(a, b) = c$, then $\frac{a}{c}$ and $\frac{b}{c}$ are

a) both prime

b) both composite

c) relatively prime to each other

d) None of these

(38) The gcd(81,135) is

- a) 3
- c) 27

- b) 9
- d) 81

(39) The $\text{lcm}(81, 135)$ is

- a) 10935
- c) 3645

- b) 2187
- d) 405

(40) The set of all real numbers under usual addition formed a group. Then the inverse of 2.36 is:

a) 2.36
c) 2.4

- b) -2.36
- d) -2.4

(41) The inverse of the element $-i$ in the multiplicative group $\{-1, 1, -i, i\}$, where $i^2 = -1$

a) i
 b) $-i$
 c) 1
 d) -1

(42) The identity element in the multiplicative group $\{-1, 1, -i, i\}$, where $i^2 = -1$

a) i b) $-i$
c) 1 d) -1

(43) A monoid $(M, +)$ is called a group if

a) $a + b = b + a = e$ b) $a + (b + c) = (a + b) + c$
 c) $a + b = b + a \forall a, b \in M$ d) $a + b \in M \quad \forall a, b \in M$

(44) A group of three element is:

- a) Always non-abelian
- b) Always abelian
- c) Sometimes abelian
- d) Always non-cyclic

(45) Let (G, \cdot) be a group and a has the inverse b then $ab^{-1} = ?$

a) σ b) α^2
 c) α d) b^2

(46) The number of elements in the group $(Z_+, +)$ is

(47) The inverse of the element [1] in the additive group Z_3

- a) [1]
- b) [2]
- c) [0]
- d) None of these

(48) If \circ denotes permutation multiplication , then the value of $(1\ 2)\circ(1\ 4)$

- a) $(4\ 1\ 2)$
- b) $(1\ 4\ 2)$
- c) $(4\ 2)$
- d) $(4\ 1)$

(49) Let α be an element in a group with order 5. Then the value of α^{2020}

- a) α
- b) α^2
- c) α^4
- d) e

(50) Let α be an element in a group with order 10. Then the order of the element α^7

- a) 10
 - b) 70
 - c) 1
 - d) Cannot be determined from the given data
- (51) Which of the following is not an abelian group:
- a) $(Q, +)$
 - b) $(Z, +)$
 - c) $(Z_3, +)$
 - d) S_5

(52) A subgroup H of a group G is normal if for all $x \in G$ and $h \in H$

- a) $xhx^{-1} \in H$
- b) $xhx^{-1} \in G$
- c) $xh^{-1} \in H$
- d) $x^{-1}h \in H$

(53) In a Boolean algebra B, if $a + b = b$ then $a.b = ?$

- a) a
- b) b
- c) a'
- d) Cannot be determined from the given data

(54) In a Boolean algebra B, $(a + b)' = ?$

- a) $a' + b'$
- b) $(a.b)'$
- c) $a'.b'$
- d) I

(55) In a Boolean algebra B, $0' = ?$

- a) I
- b) 0
- c) I'
- d) 0"

(56) Arithmetical minus (-) is a binary operation on

- a) set of all integers
- b) set of positive integers
- c) set of negative integers
- d) none

(57) A groupoid (G, \circ) is a semi-group if for all a, b, c in G

a) $\alpha \circ b = b \circ \alpha$

b) $\alpha \circ \alpha = \alpha$

c) $(\alpha \circ b) \circ c = (b \circ c) \circ \alpha$

d) $\alpha \circ (b \circ c) = (\alpha \circ b) \circ c$

(58) Which one of the following groupoid is semi-group

a) $(Z, +)$

b) $(Z, -)$

c) (R, \div)

d) None

(59) In the group $Z_4 = \{[0], [1], [2], [3]\}$ under addition $[3] + [2] =$

a) $[5]$

b) $[0]$

c) $[1]$

d) $[2]$

(60) An edge whose two end vertices coincide is called

a) ring

b) adjacent edge

c) loop

d) none