



BRAINWARE UNIVERSITY

Term End Examination 2021 - 22
Programme – Master of Science in Mathematics
Course Name – Abstract Algebra
Course Code - MSCMC201
(Semester II)

Time allotted : 1 Hrs.15 Min.

Full Marks : 60

[The figure in the margin indicates full marks.]

Group-A

(Multiple Choice Type Question)

1 x 60=60

Choose the correct alternative from the following :

- (1) Let G be a simple group of order 168. How many subgroups of G are of order 7?
 - a) 1
 - b) 7
 - c) 8
 - d) 28
- (2) A group of order 22 is
 - a) simple group
 - b) is not a simple group
 - c) commutative group
 - d) None of these
- (3) A simple group of order 63
 - a) cannot contain a subgroup of order 21
 - b) can contain a subgroup of order 21
 - c) is commutative
 - d) None of these
- (4) The direct product of two groups is commutative if and only if
 - a) both the groups are commutative.
 - b) both the groups are not commutative.
 - c) one of is commutative.
 - d) None of these
- (5) Let G be a finite group of order mn , where m and n are relatively prime. Let H and K be subgroups of G having orders m and n respectively, then $G =$
 - a) $K \times H$
 - b) $H \times K$
 - c) H
 - d) None of these
- (6) Klein 4 – group is a p – group ,where $p =$
 - a) 3
 - b) 1
 - c) 5
 - d) 2
- (7) Let G be a group of order p^2 , where p is a prime. Then G
 - a) is commutative
 - b) is noncommutative
 - c) has no subgroup of order p
 - d) None of these

- (21) Let G be a group of order 36, then G
- a) is not simple
b) is simple
c) is cyclic
d) None of these
- (22) In the ring Z of integers, the invertible element is/are
- a) only 1
b) only -1
c) both -1,1
d) only 0
- (23) The ring Z_{12} is
- a) an integral domain
b) a field
c) both integral domain and field
d) neither integral domain nor field
- (24) The ring Z_n is a field then n is always a/an
- a) even prime
b) odd prime
c) prime
d) any integer
- (25) The characteristic of the ring R of all real numbers is
- a) 0
b) 1
c) -1
d) does not exist
- (26) The characteristic of the ring C of all complex numbers is
- a) 0
b) 1
c) -1
d) does not exist
- (27) Let R be a ring with 1. Then R has characteristic n
- a) $n \cdot 1 = 1$
b) $n \cdot 1 = 0$
c) $n \cdot 1 = 1, k < n \Rightarrow k \cdot 1 \neq 1$
d) $n \cdot 1 = 0, k < n \Rightarrow k \cdot 1 \neq 0$
- (28) Which of the following is a zero of the polynomial $X^2 + \bar{2}X + \bar{1}$ in the ring Z_4 ?
- a) $\bar{0}$
b) $\bar{1}$
c) $\bar{2}$
d) No root
- (29) Let R be ring with 1. Then the $\frac{R[X]}{\langle X \rangle} =$
- a) R
b) $R[X]$
c) $R(X)$
d) $\langle X \rangle$
- (30) Let $R[X]$ be a polynomial ring and $f(X), g(X)$ be two non-zero polynomials in $R[X]$.
If $f(X) + g(X) \neq 0$ then $\max \deg(f(X), g(X))$
- a) $= \deg(f(X)) + \deg(g(X))$
b) $\geq \deg(f(X)) + \deg(g(X))$
c) $\leq \deg(f(X)) + \deg(g(X))$
d) None of these
- (31) Which of the following factor divides the polynomial $2X^2 + X + 1$ in Z_3 ?
- a) $X-1$
b) $X-2$
c) X
d) None of these
- (32) Which of the following is not a unit in the ring $Z[i]$?
- a) 0
b) 1
c) -1
d) i
- (33) Which of the following statements is true?
- a) ED implies PID
b) PID implies ED
c) ED implies and implied by PID
d) None of these
- (34) Which of the following factor divides the polynomial $2X^2 + X + 1$ in Z_5 ?
- a) $X-2$
b) $X-3$

- c) X d) None of these
- (35) The associates of $1+i$ in $Z[i]$
- a) 1 b) i
c) $1+i$ d) $-i$
- (36) The associates of $1-i$ in $Z[i]$
- a) 1 b) i
c) $1-i$ d) $-i$
- (37) Value of the $g.c.d(10,15)$ in the ring Z
- a) 1 b) 5
c) 10 d) 30
- (38) Let R be a commutative ring with 1 and A and B are two distinct maximal ideal of R then $AB=$
- a) $A+B$ b) $A \cup B$
c) $A \cap B$ d) None of these
- (39) The number of irreducible polynomial of degree two in the ring Z_2
- a) 0 b) 1
c) 2 d) 3
- (40) A rational root of the polynomial $2X^3 - 7x + 1$
- a) $1/2$ b) $2/3$
c) does not exists d) exists but none of a and b
- (41) Which of the following is an algebraic integer?
- a) i b) $1/2$
c) $i/2$ d) None of these
- (42) Let L/K be a finite extension of fields. Which of the following assertions are correct
- a) If the characteristic of K is zero, then L/K is normal b) If the characteristic of K is zero, then L/K is separable.
c) If L/K is normal, then L/K is a finite field extension d) If the characteristic of K is positive, then L/K is normal if and only if it is separable.
- (43) Which of the following is not an algebraic element over the set of all real numbers R ?
- a) π b) i
c) $\sqrt{2}$ d) None of these
- (44) The degree of i over the set of all real numbers R ?
- a) 0 b) 1
c) 2 d) 3
- (45) Which of the following field is prime?
- a) R b) Q
c) C d) $Q(\sqrt{2})$
- (46) The degree of $\sqrt{2}$ over the set of all real numbers R
- a) 0 b) 1
c) 2 d) 3

$$\mathcal{Q}(\sqrt{2}, i) \cap \mathcal{Q}(\sqrt{2} + i) = \mathcal{Q}$$

(59) Multiplicity of the root 0 of the polynomial $X^3 + 2X = 0$

- a) 3
b) 2
c) 1
d) 0

(60) Which of the following is not an irreducible polynomial with integer coefficients

- a) $X^2 + X + 1$
b) $X^2 + 1$
c) $X + 1$
d) $X^2 + 2X + 1$