

BRAINWARE UNIVERSITY

Term End Examination 2021 - 22 Programme – Master of Science in Mathematics Course Name – Operations Research Course Code - MSCMC401 (Semester IV)

Time allotted: 1 Hrs.15 Min. Full Marks: 60 [The figure in the margin indicates full marks.] Group-A (Multiple Choice Type Question) $1 \times 60 = 60$ Choose the correct alternative from the following: (1) A shop can make two types of sweets (A and B). They use two resources - flour and sugar. To make one packet of A, they need 2 kg of flour and 5 kg of sugar. To make one packet of B, they need 3 kg of flour and 3 kg of sugar. They have 25 kg of flour and 28 kg of sugar. These sweets are sold at Rs 800 and 900 per packet respectively. Find the best product mix. An appropriate objective function for this problem is to a) Maximize total revenue b) Minimize total cost c) Maximize the total units of products d) None of these produced. (2) A shop can make two types of sweets (A and B). They use two resources - flour and sugar. To make one packet of A, they need 2 kg of flour and 5 kg of sugar. To make one packet of B, they need 3 kg of flour and 3 kg of sugar. They have 25 kg of flour and 28 kg of sugar. These sweets are sold at Rs 800 and 900 per packet respectively. Find the best product mix. The number of decision variables is a) 1 b) 2 d) 4 c) 3

b) 2

d) 4

A company makes two products (A and B) and both require processing on 2 machines. Product A takes 10 and 15 minutes on the two machines per unit and product B takes 22 and 18 minutes per unit on the two machines. Both the machines are available for 2640 minutes per week. The products are sold for Rs 200 and Rs 175 respectively per unit. Formulate a LP to maximize revenue? The market can take a maximum of 150

units of product.

a) 1c) 3

The number of decision variables is

Product A takes 10 and 15 minutes 22 and 18 minutes per unit on the 2640 minutes per week. The produ	a and B) and both require processing on 2 machines. s on the two machines per unit and product B takes two machines. Both the machines are available for acts are sold for Rs 200 and Rs 175 respectively per revenue? The market can take a maximum of 150	
a) 1	b) 2	
c) 4	d) 5	
An investor has Rs 20 lakhs with her and considers three schemes to invest the money for one year. The expected returns are 10%, 12% and 15% for the three schemes per year. The third scheme accepts only up to 10 lakhs. The investor wants to invest more money in scheme 1 than in scheme 2. The investor assesses the risk associated with the three schemes as 0 units, 10 units and 20 units per lakh invested and does not want her risk to exceed 500 units. How many constraints are in your formulation?		
a) 2	b) 3	
c) 4	d) 5	
Two tasks have to be completed and require 10 hours and 12 hours of work if one person does the tasks. If n people do task 1, the time to complete the task becomes 10/n and so on. Similarly if n people do task 2, the time becomes 12/n and so on. We have 5 people and they have to be assigned to the two tasks. We cannot assign more than three to task 1. Find the earliest time that both tasks are completed if they start at the same time. (Use ideas from the bicycle problem to write your objective function. At some point you may have to define a variable to represent the reciprocal of another variable). Formulate an LP problem and answer the following: The final objective function is		
a) Maximization problem with one ten objective function	rm in the b) Minimization problem with one term in the objective function	
c) Maximization problem with two tenthe objective function	rms in d) Minimization problem with two terms in the objective function	
Two tasks have to be completed and require 10 hours and 12 hours of work if one person does the tasks. If n people do task 1, the time to complete the task becomes 10/n and so on. Similarly if n people do task 2, the time becomes 12/n and so on. We have 5 people and they have to be assigned to the two tasks. We cannot assign more than three to task 1. Find the earliest time that both tasks are completed if they start at the same time. (Use ideas from the bicycle problem to write your objective function. At some point you may have to define a variable to represent the reciprocal of another variable). Formulate an LP problem and answer the following: The total number of constraints in the final formulation is		
a) 1	b) 2	
c) 3	d) 4	
	three factories to three retail stores. The available pectively in the three factories and the requirements	

TV sets are to be transported from three factories to three retail stores. The available quantities are 300, 400 and 500 respectively in the three factories and the requirements are 250, 350 and 500 in the three stores. They are first transported from the factories to warehouses and then sent to the retail stores. There are two warehouses and their capacities are 600 and 700 units. The unit costs of transportation from the factories to warehouses and from the warehouses to retail stores are known. Formulate an LP and answer the following questions:

The objective function

- Maximizes the total cost of transportation between factories and warehouses and between warehouses and retail stores
- Maximizes the total quantity transported between factories and warehouses and between warehouses and retail stores
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The number of terms in the objective function is

a) 6

b) 8

d)

c) 12

d) 18

(10)

TV sets are to be transported from three factories to three retail stores. The available quantities are 300, 400 and 500 respectively in the three factories and the requirements are 250, 350 and 500 in the three stores. They are first transported from the factories to warehouses and then sent to the retail stores. There are two warehouses and their capacities are 600 and 700 units. The unit costs of transportation from the factories to warehouses and from the warehouses to retail stores are known. Formulate an LP and answer the following questions:

The number of decision variables in the formulation is

a) 8

b) 10

c) 12

d) 18

Thousand answer papers have to be totaled in four hours. There are 10 regular teachers, 5 staff and 4 retired teachers who can do the job. Regular teachers can total 20 papers in an hour; staff can do 15 per hour while retired teachers can do 18 per hour. The regular teachers total the papers correctly 98% of the times while this number is 94% and 96% for staff and retired teachers. We have to use the services of at least one staff. You can assume that any person can work for a fraction of an hour also. Formulate a relevant LP problem and answer the following questions. A relevant objective function would be to

- a) Maximize the papers totaled by all of them in four hours
- b) Minimize the papers totaled by staff and retired teachers
- c) Minimize the number of papers correctly totaled by all of them
- d) Minimize the number of papers incorrectly totaled by all of them
- Thousand answer papers have to be totaled in four hours. There are 10 regular teachers, 5 staff and 4 retired teachers who can do the job. Regular teachers can total 20 papers in an hour; staff can do 15 per hour while retired teachers can do 18 per hour. The regular teachers total the papers correctly 98% of the times while this number is 94% and 96% for staff and retired teachers. We have to use the services of at least one staff. You can assume that any person can work for a fraction of an hour also. Formulate a relevant LP problem and answer the following questions.

The number of decision variables in an efficient formulation is

a) 3

b) 4

c) 9

d) 19

(13)

A person is in the business of buying and selling items. He has 10 units in stock and plans for the next three periods. He can buy the item at the rate of Rs 50, 55 and 58 at the beginning of periods 1, 2 and 3 and can sell them at Rs 60, 64 and 66 at the end of the three periods. He can use the money earned by selling at the end of the period to buy items at the beginning of the next period. He can buy a maximum of 200 per period. He can borrow money at the rate of 2% per period at the beginning of each period. He can borrow a maximum of Rs 8000 per period and he cannot borrow more than Rs 20000 in total. He has to pay back all the loans with interest at the end of the third period.

What is the correct objective function for this problem?

- a) Maximize the total money available at the end of the third period
- c) Maximize the total money at the end of the third period less total money paid back including interest
- Maximize the total money at the end of the third period less total money borrowed
- d)
 Maximize the number of items sold at
 the end of the third period

(14)

A food stall sells idlis, dosas and poories. A plate of idli has 2 pieces, a plate of dosa has 1 piece while a plate of poori has 2 pieces. They also sell a "combo" which has 2 idlis and 2 poories. A kg of batter costs Rs 60 and contains twelve spoons of batter. Each piece of idli requires 1 spoon of batter and each dosa requires 1.5 spoons of batter. Each poori piece requires 1 ball of wheat dough and a kg of wheat dough that costs Rs 60 can make 20 balls of dough. The selling prices of the items are Rs 40, 60, 60 and 90 per plate respectively. The owner has Rs 800 with her and estimates the demand for the four items (in plates) as 50, 30, 20 and 10 respectively. There is a penalty cost of Rs 10 for any unmet plate of demand of an item. Idli being the most commonly consumed item, the owner wishes to meet at least 80% of the demand. Formulate an LP problem and answer the following questions: What is the most suitable objective function for this problem?

- a) Maximize the total money earned by sale
- c) Maximize the total plates made of all the items

- b) Maximize the total money earned by sale less the cost of items bought
- d) Minimize the unmet demand

(15)

A food stall sells idlis, dosas and poories. A plate of idli has 2 pieces, a plate of dosa has 1 piece while a plate of poori has 2 pieces. They also sell a "combo" which has 2 idlis and 2 poories. A kg of batter costs Rs 60 and contains twelve spoons of batter. Each piece of idli requires 1 spoon of batter and each dosa requires 1.5 spoons of batter. Each poori piece requires 1 ball of wheat dough and a kg of wheat dough that costs Rs 60 can make 20 balls of dough. The selling prices of the items are Rs 40, 60, 60 and 90 per plate respectively. The owner has Rs 800 with her and estimates the demand for the four items (in plates) as 50, 30, 20 and 10 respectively. There is a penalty cost of Rs 10 for any unmet plate of demand of an item. Idli being the most commonly consumed item, the owner wishes to meet at least 80% of the demand. Formulate an LP problem and answer the following questions:

How many decision variables are in the formulation

a) 3

b) 4

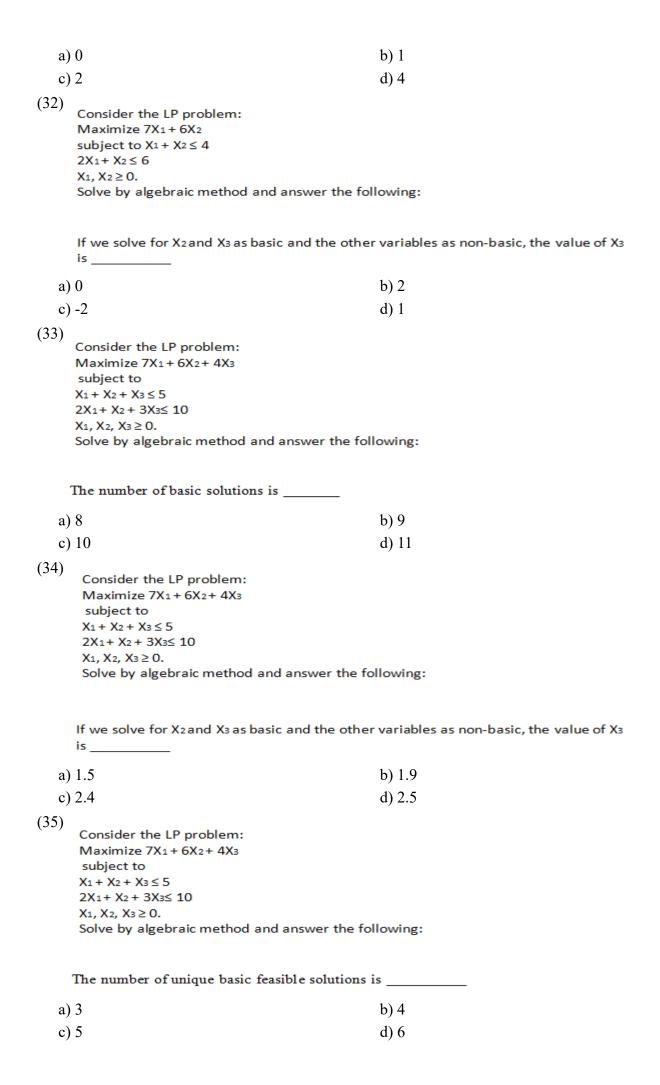
c) 5

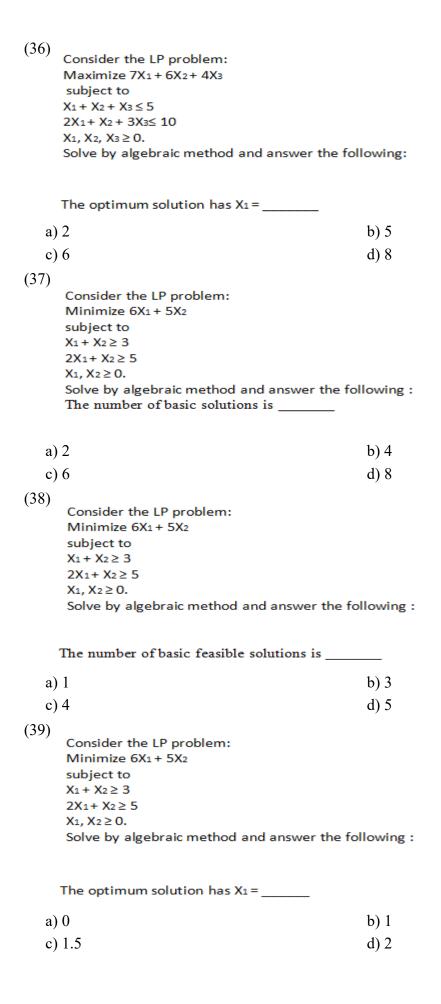
d) 8

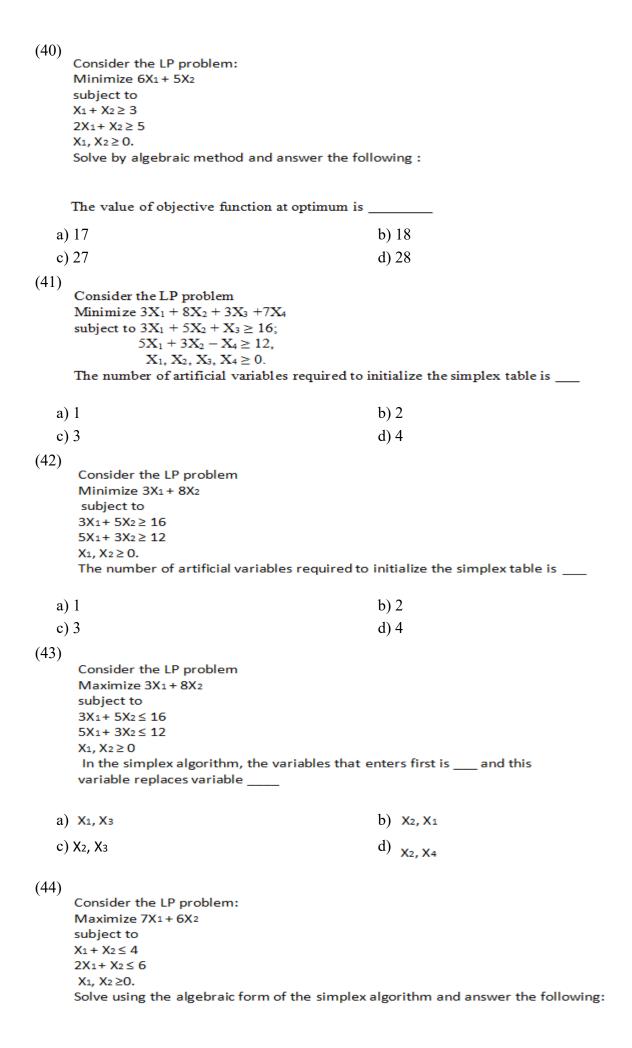
(16)	A food stall sells idlis, dosas and poories. A plate of idli has 2 pieces, a plate of dosa has 1 piece while a plate of poori has 2 pieces. They also sell a "combo" which has 2 idlis and 2 poories. A kg of batter costs Rs 60 and contains twelve spoons of batter. Each piece of idli requires 1 spoon of batter and each dosa requires 1.5 spoons of batter. Each poori piece requires 1 ball of wheat dough and a kg of wheat dough that costs Rs 60 can make 20 balls of dough. The selling prices of the items are Rs 40, 60, 60 and 90 per plate respectively. The owner has Rs 800 with her and estimates the demand for the four items (in plates) as 50, 30, 20 and 10 respectively. There is a penalty cost of Rs 10 for any unmet plate of demand of an item. Idli being the most commonly consumed item, the owner wishes to meet at least 80% of the demand. Formulate an LP problem and answer the following questions:			
	How many constraints are in the formulation			
a)) 3	b) 4		
c)) 5	d) 6		
(17) Consider the maximum flow problem with n nodes and m arcs. You are writing a formulation with f as the maximum flow.				
	The total number of constraints is	_		
a)) m	b) n		
c)) m+n	d) m.n		
(18) Consider the napkins problem where the requirement is for 20 days. There are two types of laundries – fast and slow. The fast laundry takes 2 days (napkins sent at the end of day 1 can be used on day 3) and the slow laundry takes 3 days (napkins sent at the end of day 1 can be used on day 4). The costs of the new napkins and the two laundries are known. The objective function has terms				
a)) 54	b) 55		
c)) 56	d) 57		
(19)	Consider the napkins problem where the requirement is for 20 days. There are two types of laundries – fast and slow. The fast laundry takes 2 days (napkins sent at the end of day 1 can be used on day 3) and the slow laundry takes 3 days (napkins sent at the end of day 1 can be used on day 4). The costs of the new napkins and the two laundries are known.			
	The total number of variables in the formulation	on is		
a)) 58	b) 57		
c)) 55	d) 53		
(20)	O) Consider the napkins problem where the requirement is for 20 days. There are two types of laundries — fast and slow. The fast laundry takes 2 days (napkins sent at the end of day 1 can be used on day 3) and the slow laundry takes 3 days (napkins sent at the end of day 1 can be used on day 4). The costs of the new napkins and the two laundries are known.			
	The constraint to meet the demand of day 10 v	vill have terms		
a)) 20	b) 25		
) 30	d) 35		

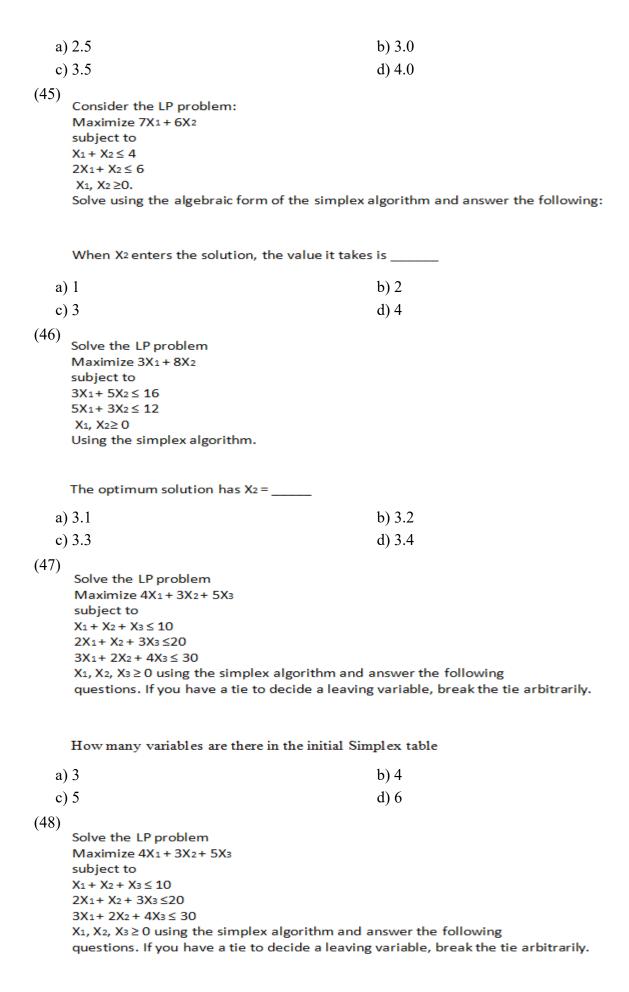
(21) Consider the media selection problem with n possible things to invest in. Examples could be TV, radio, newspaper etc. There is a total budget restriction and limit on investment in each. The objective function has terms			
a)	n	b) n+1	
	n+2	d) n-1	
		,	
(22) Consider the media selection problem with n possible things to invest in. Examples could be TV, radio, newspaper etc. There is a total budget restriction and limit on investment in each.			
	The number of decision variables is	_	
a)	n-1	b) n-2	
c)	n	d) n+1	
(23)	Consider the LP problem: Maximize $7X_1 + 6X_2$ subject to $X_1 + X_2 \le 4$ $2X_1 + X_2 \le 6$ $X_1, X_2 \ge 0$ The objective function corresponding to the x_1	optimum solution is	
a)	24	b) 26	
,	28	d) 30	
(24)	Consider the LP problem: Maximize $5X_1 + 8X_2$ subject to $3X_1 + 4X_2 \le 12$ $5X_1 + 2X_2 \le 20$ $X_1, X_2 \ge 0$. The objective function corresponding to the	optimum solution is	
a)	24	b) 26	
,	30	d) 36	
	A constraint that does not affect the feasible re	,	
a)	non-negativity constraint	b) slack constraint	
c)	redundant constraint	d) standard constraint	
(26)	Consider the LP problem: Maximize $5X_1 + 8X_2$ subject to $2X_1 + 3X_2 \le 8$ $2X_1 + 3X_2 \ge -1$ $X_1, X_2 \ge 0$. The corner point that gives the optimum solution	tion is	
a)	(0,8/3)	b) (8/3,0)	
c)	(0,3/8)	d) (3/8,0)	

(27) Consider the LP problem:	
Maximize $7X_1 + 6X_2$ subject to $X_1 \le 4$	
X1 - X2 ≥ 0	
$X_1, X_2 \ge 0$	
The objective function correspondin	g to the optimum solution is
a) 48	b) 49
c) 51	d) 52
28)	
Consider the LP problem:	
Minimize 5X1 + 8X2	
subject to $X_1 + X_2 \le 6$	
$X_1 + X_2 \ge 2$	
X₁ - X₂≤ 2	
X ₁ - X ₂ ≥ -2	
$X_1, X_2 \ge 0$. The objective function value at opting	mum is
The objective failution value at opti-	
a) 6	b) 7
c) 8	d) 10
29)	
Consider the LP problem:	
Minimize 2X1 - 3X2	
subject to X1 + X2 ≤ 4	
$2X_1 + X_2 \ge 2$	
$X_1 + 2X_2 \le 6$	
$X_1, X_2 \ge 0$. The objective function value at optin	num is
The objective function value at optim	
a) -7	b) -9
c) 7	d) 9
30)	
Consider the LP problem:	
Maximize $7X_1 + 6X_2$ subject to $X_1 + X_2 \le 4$	
2X ₁ + X ₂ ≤ 6	
$X_1, X_2 \ge 0.$	
Solve by algebraic method and answe	er the following:
The number of basic feasible solution	s is
a) 1	b) 2
c) 3	d) 4
,	a) .
31) Consider the LP problem:	
Maximize 7X1 + 6X2	
subject to $X_1 + X_2 \le 4$ $2X_1 + X_2 \le 6$	
X ₁ , X ₂ ≥ 0.	
Solve by algebraic method and answe	er the following:
If we solve for X1 and X3 as basic and	the other variables as non-basic, the value of
is	



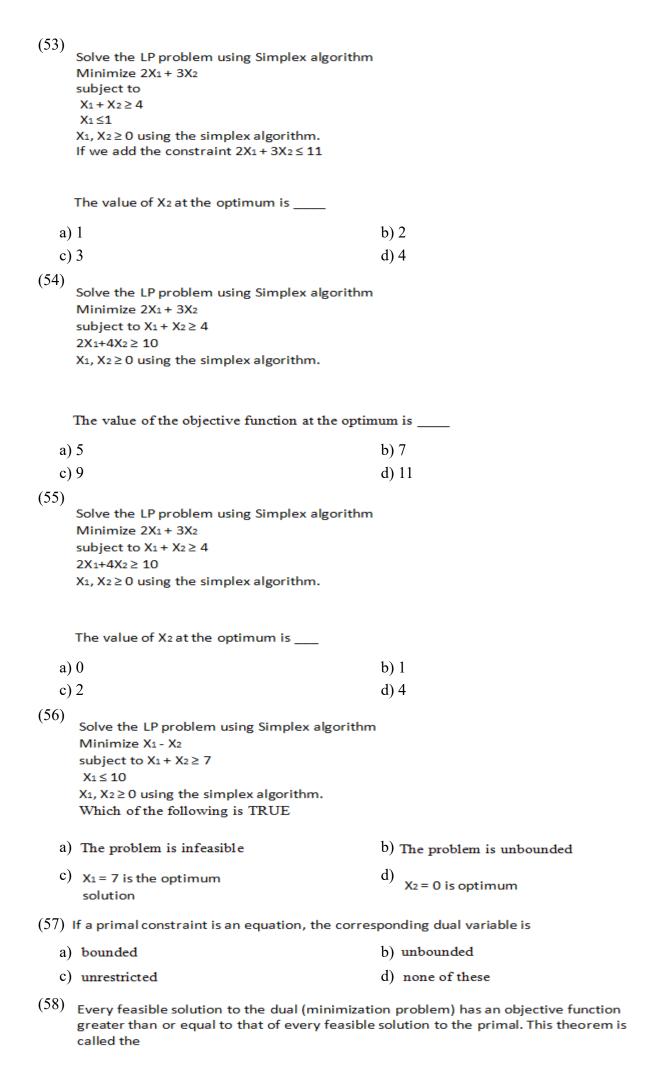






How many basic variables have a positive value at the optimum

a)	1	b) 2
c)	3	d) 5
(49)		
	Solve the LP problem	
	Maximize 4X1 + 3X2 + 5X3 subject to	
	$X_1 + X_2 + X_3 \le 10$	
	$2X_1 + X_2 + 3X_3 \le 20$ $3X_1 + 2X_2 + 4X_3 \le 30$	
	$X_1, X_2, X_3 \ge 0$ using the simplex algorithm and	answer the following
	questions. If you have a tie to decide a leavin	g variable, break the tie arbitrarily.
	How many $C_j - Z_j$ values are zero at the optim	num
a)	1	b) 2
c)	3	d) 4
(50)		,
(00)	Solve the LP problem Maximize 9X1 + 3X2 + 5X3	
	subject to	
	$4X_1 + X_2 + X_3 \le 12$	
	$2X_1 + 4X_2 + 3X_3 \le 22$ $5X_1 + 2X_2 + 4X_3 \le 34$	
	$X_1, X_2, X_3 \ge 0$ using the simplex algorithm and	answer the following questions.
	The number of iterations taken by simplex (af	ter the initial table) to reach the
	optimum is	
a)	1	b) 2
	3	d) 4
(51)		,
(01)	Solve the LP problem	
	Maximize 9X1 + 3X2 + 5X3 subject to	
	$4X_1 + X_2 + X_3 \le 12$	
	$2X_1 + 4X_2 + 3X_3 \le 22$ $5X_1 + 2X_2 + 4X_3 \le 34$	
	$X_1, X_2, X_3 \ge 0$ using the simplex algorithm and	answer the following questions.
	The set of basic variables at the optimum is	
a)	X1 X2 X6	b) X1 X3 X5
	X ₁ X ₃ X ₆	d) _{X2 X3 X6}
•)	ALAGAO	X2 X3 X6
(52)		
	Solve the LP problem using Simplex algorithm Minimize 2X1 + 3X2	ו
	subject to	
	$X_1 + X_2 \ge 4$ $X_1 \le 1$	
	X1, X2≥0 using the simplex algorithm.	
	If we add the constraint $2X_1 + 3X_2 \le 11$	
	The value of the objective function at the opti	mum is
	,	
a)	7	b) 9
	10	d) 11



	a) Weak duality theorem	O) Optimality criterion theorem
	c) Main duality theorem	d) Complimentary slackness theorem
(59	In the optimum solution, if a primal constrain of the corresponding dual variable is	t is satisfied as an equation, the value
	a) Positive	b) Negative
	c) Zero	d) Can't be said.
(60	If the k th variable in a minimization (primal) is inequality of the type	\geq 0, the k^{th} constraint in the dual is an
	a) ≥	b) <
	c) ₌	d) Can't be said.